

## CLAIMS

What is claimed is:

1. A method of obtaining predictive information for inhomogeneous financial time series, comprising the steps of:
  - 5 electronically receiving financial market transaction data over an electronic network;
  - electronically storing in a computer-readable medium said received financial market transaction data;
  - constructing an inhomogeneous time series  $z$  that represents said received financial market transaction data;
  - 10 constructing an exponential moving average operator;
  - constructing an iterated exponential moving average operator based on said exponential moving average operator;
  - constructing a time-translation-invariant, causal operator  $\Omega[z]$  that is a convolution operator with kernel  $\omega$  and that is based on said iterated exponential moving average operator;
  - 15 electronically calculating values of one or more predictive factors relating to said time series  $z$ , wherein said one or more predictive factors are defined in terms of said operator  $\Omega[z]$ ; and
  - electronically storing in a computer readable medium said calculated values of one or 20 more predictive factors.

2. The method of claim 1, wherein said operator  $\Omega[z]$  has the form:

$$\begin{aligned} \Omega[z](t) &= \int_{-\infty}^t dt' \omega(t-t') z(t') \\ 25 &= \int_0^\infty dt' \omega(t') z(t-t'). \end{aligned}$$

3. The method of claim 1, wherein said exponential moving average operator  $EMA[\tau ; z]$  has the form:

$$\begin{aligned} 30 \quad EMA[\tau ; z](t_n) &= \mu EMA(\tau ; z)(t_{n-1}) + (\nu - \mu) z_{n-1} + (1 - \nu) z_n, \text{ with} \\ \alpha &= \frac{\tau}{t_n - t_{n-1}}, \\ \mu &= e^{-\alpha}, \end{aligned} \tag{23}$$

where  $v$  depends on a chosen interpolation scheme.

4. The method of claim 1, wherein said operator  $\Omega[z]$  is a differential operator  
5  $\Delta[\tau]$  that has the form:

$$\Delta[\tau] = \gamma(\text{EMA}[\alpha\tau, 1] + \text{EMA}[\alpha\tau, 2] - 2 \text{EMA}[\alpha\beta\tau, 4]),$$

where  $\gamma$  is fixed so that the integral of the kernel of the differential operator from the origin to the first zero is 1;  $\alpha$  is fixed by a normalization condition that requires  $\Delta[\tau; c] = 0$  for a

- 10 constant  $c$ ; and  $\beta$  is chosen in order to get a short tail for the kernel of the differential operator  
 $\Delta[\tau]$ .

5. The method of claim 4 wherein said one or more predictive factors comprises  
a return of the form  $r[\tau] = \Delta[\tau; x]$ , where  $x$  represents a logarithmic price.

- 15 6. The method of claim 1 wherein said one or more predictive factors comprises  
a momentum of the form  $x - \text{EMA}[\tau; x]$ , where  $x$  represents a logarithmic price.

7. The method of claim 1 wherein said one or more predictive factors comprises  
20 a volatility.

8. The method of claim 7 wherein said volatility is of the form:

$$\text{Volatility } [\tau, \tau'; p; z] = \text{MNorm } [\tau/2, p; \Delta[\tau'; z]], \quad \text{where}$$

$$25 \quad \text{MNorm}[\tau, p; z] = \text{MA}[\tau; |z|^p]^{1/p}, \quad \text{and}$$

$$\text{MA}[\tau, n] = \frac{1}{n} \sum_{k=1}^n \text{EMA}[\tau', k], \quad \text{with } \tau' = \frac{2\tau}{n+1}, \quad \text{and where } p \text{ satisfies } 0 < p \leq 2,$$

- 30 and  $\tau'$  is a time horizon of a return  $r[\tau] = \Delta[\tau; x]$ , where  $x$  represents a logarithmic price.

9. A method of obtaining predictive information for inhomogeneous financial time series, comprising the steps of:
- electronically receiving financial market transaction data over an electronic network;
  - electronically storing in a computer readable medium said received financial market transaction data;
  - constructing an inhomogeneous time series  $z$  that corresponds to said received financial market transaction data;
  - constructing an exponential moving average operator;
  - constructing an iterated exponential moving average operator based on said exponential moving average operator;
  - constructing a time-translation-invariant, causal operator  $\Omega[z]$  that is a convolution operator with kernel  $\omega$  and that is based on said iterated exponential moving average operator;
  - constructing a standardized time series  $\hat{z}$ ;
  - electronically calculating values of one or more predictive factors relating to said time series  $z$ , wherein said one or more predictive factors are defined in terms of said standardized time series  $\hat{z}$ ; and
  - electronically storing in a computer readable medium said calculated values of one or more predictive factors.
10. The method of claim 9 wherein the standardized time series  $\hat{z}$  is of the form:
- $$\hat{z}[\tau] = \frac{z - MA[\tau;z]}{MSD[\tau;z]}, \text{ where}$$
- 25  $MA[\tau,n] = \frac{1}{n} \sum_{k=1}^n EMA[\tau',k], \quad \text{with } \tau' = \frac{2\tau}{n+1}, \quad \text{and}$
- where  $MSD[\tau,p;z] = MA[\tau;|z - MA[\tau;z]|^p]^{1/p}$ .
11. The method of claim 9 wherein said one or more predictive factors comprises a moving skewness.
- 30 12. The method of claim 11 wherein said moving skewness is of the form:

MSkewness $[\tau_1, \tau_2; z] = \text{MA}[\tau_1; \hat{z}[\tau_2]]$  where  $\tau_1$  is the length of a time interval around time “now” and  $\tau_2$  is the length of a time interval around time “now –  $\tau$ ”.

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13. The method of claim 12 wherein the standardized time series  $\hat{z}$  is of the form:

$$\hat{z}[\tau] = \frac{z - \text{MA}[\tau; z]}{\text{MSD}[\tau; z]}, \text{ where}$$

$$10 \quad \text{MA}[\tau, n] = \frac{1}{n} \sum_{k=1}^n \text{EMA}[\tau', k], \quad \text{with } \tau' = \frac{2\tau}{n+1}, \quad \text{and}$$

$$\text{where } \text{MSD}[\tau, p; z] = \text{MA}[\tau; |z - \text{MA}[\tau; z]|^p]^{1/p}.$$

14. The method of claim 9 wherein said one or more predictive factors comprises  
15 a moving kurtosis.

15. The method of claim 14 wherein said moving kurtosis is of the form

$$\text{MKurtosis}[\tau_1, \tau_2; z] = \text{MA}[\tau_1; \hat{z}[\tau_2]^4], \quad \text{where } \tau_1 \text{ is the length of a time interval}$$

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around time “now” and  $\tau_2$  is the length of a time interval around time “now –  $\tau$ .”

16. The method of claim 15 wherein the standardized time series  $\hat{z}$  is of the form:

$$25 \quad \hat{z}[\tau] = \frac{z - \text{MA}[\tau; z]}{\text{MSD}[\tau; z]}, \text{ where}$$

$$\text{MA}[\tau, n] = \frac{1}{n} \sum_{k=1}^n \text{EMA}[\tau', k], \quad \text{with } \tau' = \frac{2\tau}{n+1}, \quad \text{and}$$

$$\text{where } \text{MSD}[\tau, p; z] = \text{MA}[\tau; |z - \text{MA}[\tau; z]|^p]^{1/p}.$$

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17. A method of obtaining predictive information for inhomogeneous financial time series, comprising the steps of:

- electronically receiving financial market transaction data over an electronic network;  
electronically storing in a computer readable medium said received financial market  
transaction data;
- constructing an inhomogeneous time series  $z$  that corresponds to said received  
5 financial market transaction data;
- constructing an exponential moving average operator  $\text{EMA}[\tau ; z]$ ;
- constructing an iterated exponential moving average operator based on said  
exponential moving average operator  $\text{EMA}[\tau ; z]$ ;
- constructing a time-translation-invariant, causal operator  $\Omega[z]$  that is a convolution  
10 operator with kernel  $\omega$  and time range  $\tau$ , and that is based on said iterated exponential moving  
average operator;
- constructing a moving average operator  $\text{MA}$  that depends on said  $\text{EMA}$  operator;
- constructing a moving standard deviation operator  $\text{MSD}$  that depends on said  $\text{MA}$   
operator;
- 15 electronically calculating values of one or more predictive factors relating to said time  
series  $z$ , wherein said one or more predictive factors depend on one or more of said operators  
 $\text{EMA}$ ,  $\text{MA}$ , and  $\text{MSD}$ ; and
- electronically storing in a computer readable medium said calculated values of one or  
more predictive factors.
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18. The method of claim 17 wherein said one or more predictive factors comprises  
a moving correlation.
19. The method of claim 18 wherein said moving correlation is of the form:
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- $$\text{MCorrelation}[\hat{y}, \hat{z}](t) = \int_0^\infty \int_0^\infty dt' dt'' c(t', t'') \hat{y}(t-t') \hat{z}(t-t'') .$$
20. A method of obtaining predictive information for inhomogeneous financial  
time series, comprising the steps of:
- 30 electronically receiving financial market transaction data over an electronic network;  
electronically storing in a computer readable medium said received financial market  
transaction data;

constructing an inhomogeneous time series  $z$  that corresponds to said received financial market transaction data;

constructing a complex iterated exponential moving average operator  $\text{EMA}[\tau; z]$ , with kernel  $\text{ema}$ ;

5       constructing a time-translation-invariant, causal operator  $\Omega[z]$  that is a convolution operator with kernel  $\omega$  and time range  $\tau$ , and that is based on said complex iterated exponential moving average operator;

constructing a windowed Fourier transform  $\text{WF}$  that depends on said  $\text{EMA}$  operator;  
electronically calculating values of one or more predictive factors relating to said time  
10 series  $z$ , wherein said one or more predictive factors depend on said windowed Fourier transform; and

electronically storing in a computer readable medium said calculated values of one or more predictive factors.

15       21.     The method of claim 20 wherein said complex iterated exponential moving average operator  $\text{EMA}$  has a kernel  $\text{ema}$  of the form:

$$\text{ema}[\zeta, n](t) = \frac{1}{(n-1)!} \left( \frac{t}{\tau} \right)^{n-1} \frac{e^{-\zeta t}}{\tau}, \text{ where } \zeta \in \mathbb{C}, \text{ with } \zeta = \frac{1}{\tau}(1 + ik).$$

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22.     The method of claim 20 wherein  $\text{EMA}$  is computed using the iterative computational formula:

$$\begin{aligned} \text{EMA}[\zeta; z](t_n) &= \mu \text{EMA}[\zeta; z](t_{n-1}) + z_{n-1} \frac{\nu - \mu}{1 + ik} + z_n \frac{1 - \nu}{1 + ik}, \text{ with} \\ &\alpha = \zeta(t_n - t_{n-1}) \\ &\mu = e^{-\alpha} \end{aligned}$$

where  $\nu$  depends on a chosen interpolation scheme.

23.     The method of claim 20 wherein said windowed Fourier transform has a  
30 kernel  $\text{wf}$  of the form:

$$\text{wf}[\tau, k, n](t) = \frac{1}{n} \sum_{j=1}^n \text{ema}[\zeta, j](t).$$

24. The method of claim 23 wherein said ema is of the form:

$$5 \text{ ema}[\zeta, n](t) = \frac{1}{(n-1)!} \left( \frac{t}{\tau} \right)^{n-1} \frac{e^{-\zeta t}}{\tau}, \text{ where } \zeta \in \mathbb{C}, \text{ with } \zeta = \frac{1}{\tau}(1 + ik).$$

25. A method of obtaining predictive information for inhomogeneous time series, comprising the steps of:

electronically receiving time series data over an electronic network;

10 electronically storing in a computer-readable medium said received time series data;

constructing an inhomogeneous time series  $z$  that represents said time series data;

constructing an exponential moving average operator;

constructing an iterated exponential moving average operator based on said exponential moving average operator;

15 constructing a time-translation-invariant, causal operator  $\Omega[z]$  that is a convolution operator with kernel  $\omega$  and that is based on said iterated exponential moving average operator;

electronically calculating values of one or more predictive factors relating to said time series  $z$ , wherein said one or more predictive factors are defined in terms of said operator

20  $\Omega[z]$ ; and

electronically storing in a computer readable medium said calculated values of one or more predictive factors.